

ALLIANCE

General Certificate of Education

Mathematics 6360

MM04 Mechanics 4

Mark Scheme

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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М	mark is for method						
m or dM	mark is dependent on one or more M marks and is for method						
А	mark is dependent on M or m marks and is for accuracy						
В	mark is independent of M or m marks and is for method and accuracy						
E	mark is for explanation						
or ft or F	follow through from previous						
	incorrect result	MC	mis-copy				
CAO	correct answer only	MR	mis-read				
CSO	correct solution only	RA	required accuracy				
AWFW	anything which falls within	FW	further work				
AWRT	anything which rounds to	ISW	ignore subsequent work				
ACF	any correct form	FIW	from incorrect work				
AG	answer given	BOD	given benefit of doubt				
SC	special case	WR	work replaced by candidate				
OE	or equivalent	FB	formulae book				
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme				
–x EE	deduct <i>x</i> marks for each error	G	graph				
NMS	no method shown	c	candidate				
PI	possibly implied	sf	significant figure(s)				
SCA	substantially correct approach	dp	decimal place(s)				

Key to mark scheme and abbreviations used in marking

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

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			Ν	MM04 - AQA GCE Mark Scheme 2007 June
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Q	Solution	Mark	Total	Comments
1(a)(i)	$ \begin{pmatrix} 1\\2\\3 \end{pmatrix} + \begin{pmatrix} 4\\-3\\5 \end{pmatrix} + \mathbf{F} = \begin{pmatrix} 0\\0\\0 \end{pmatrix} $	M1		sum of forces = 0 must be seen for M1
	$\Rightarrow \mathbf{F} = \begin{pmatrix} -5\\1\\-8 \end{pmatrix}$	B1 A1	3	$\pm (5\mathbf{i} - \mathbf{j} + 8\mathbf{k})$ seen correct sign
(ii)	$\left \mathbf{F}\right = \sqrt{5^2 + 1^2 + 8^2} = \sqrt{90} = 3\sqrt{10}$	M1		$\sqrt{\text{their } \mathbf{F} \text{ components}}$
(h)	$Moment = \mathbf{r} \times \mathbf{F}$	AI	2	AG
	$\begin{vmatrix} \mathbf{i} & 1 & 1 \\ \mathbf{j} & -1 & 2 \\ \mathbf{k} & 6 & 3 \end{vmatrix} + \begin{vmatrix} \mathbf{i} & 0 & 4 \\ \mathbf{j} & 3 & -3 \\ \mathbf{k} & -2 & 5 \end{vmatrix} + \begin{vmatrix} \mathbf{i} & 0 & -5 \\ \mathbf{j} & 3 & 1 \\ \mathbf{k} & -2 & -8 \end{vmatrix}$	M1 M1		attempt at one r × F (all attempted)
	$= \begin{pmatrix} -15\\3\\3 \end{pmatrix} + \begin{pmatrix} 9\\-8\\-12 \end{pmatrix} + \begin{pmatrix} -22\\10\\15 \end{pmatrix}$	A1√ A1√		any three components correct all components correct
	$= \begin{pmatrix} -28\\5\\6 \end{pmatrix}$	A1√	5	sum of vectors; \checkmark their F from part (a)
	1 st Alternative for (b):			
	$\overrightarrow{QP} = \begin{pmatrix} 1\\ -4\\ 8 \end{pmatrix}$	(M1) (A1)		intention to use $\mathbf{r} \times \mathbf{F}$ about Q \overrightarrow{QP} obtained correctly
	Moments about <i>O</i>			
	$ i \ 1 \ 1 \ (-28)$	(M1)		determinant attempted
	$QP \times \mathbf{F}_1 = \begin{vmatrix} \mathbf{j} & -4 & 2 \end{vmatrix} = \begin{vmatrix} 5 \end{vmatrix}$	(A1)		one component correct
	$ \mathbf{k} \ 8 \ 3 \ (6)$	(A1)	(5)	all correct
	2 nd Alternative for (b):			
	$\overrightarrow{PQ} = \begin{pmatrix} -1\\4\\-8 \end{pmatrix}$	(M1) (A1)		intention to use $\mathbf{r} \times \mathbf{F}$ about <i>P</i> \overrightarrow{PQ} obtained correctly
	$\begin{vmatrix} \mathbf{i} & -1 & -5 \\ \mathbf{j} & 4 & 1 \\ \mathbf{k} & -8 & -8 \end{vmatrix} = \begin{pmatrix} -24 \\ 32 \\ 19 \end{pmatrix}$	(M1)		one determinant correct
	$\begin{vmatrix} \mathbf{i} & -1 & 4 \\ \mathbf{j} & 4 & -3 \\ \mathbf{k} & -8 & 5 \end{vmatrix} = \begin{pmatrix} -4 \\ -27 \\ -13 \end{pmatrix}$	(A1)		both correct
	$ \begin{pmatrix} -24\\ 32\\ 19 \end{pmatrix} + \begin{pmatrix} -4\\ -27\\ -13 \end{pmatrix} = \begin{pmatrix} -28\\ 5\\ 6 \end{pmatrix} $	(A1)	(5)	all correct
	Total		10	

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104 (cont))	1		40
Q	Solution	Mark	Total	Comments
2(a)	volume = $\pi \int y^2 dx$			
	$=\pi\int_{0}^{2}\left(4-x^{2}\right)\mathrm{d}x$	M1		evidence of attempt at $\int y^2 dx$
	$\begin{bmatrix} x^3 \end{bmatrix}^2$			
	$=\pi \left[4x - \frac{1}{3} \right]_0$	A1		integrating
	$=\pi\left[8-\frac{8}{3}-0\right]$			
	$=\frac{16\pi}{2}$	A1	3	AG
	3			
(b)	$\frac{16\pi}{3}\overline{x} = \pi \int_0^2 x(4-x^2) \mathrm{d}x$			
	$=\pi\int_0^2 (4x-x^3) \mathrm{d}x$	M1		attempt at $\int xy^2 dx$
	$=\pi\left[2x^2-\frac{x^4}{x^4}\right]^2$	A1		integrating correctly
	$=\pi[8-4-0]$	m1		equation to find \overline{x} (dependent on first M1)
	$=4\pi$			
	$\Rightarrow \overline{x} = \frac{5}{4}$	A1	4	
(c)				
	3			
	$\tan\theta = \frac{\overline{4}}{2}$	M1		$\tan\theta$ seen
	_3	Δ1 Δ		structure correct \overline{x}
	$\overline{8}$		2	Structure correct $\frac{1}{2}$
	$\rightarrow \sigma = 20.0^{\circ}$	Al√	<u> </u>	accept AWFW $20^{\circ} - 21^{\circ}$; \checkmark their x

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Q	Solution	Mark	Total	Comments
3(a)(i)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$			
	Resolve vertically at <i>B</i> :			
	$T_1 \sin 45^\circ + 500 = 0$	M1A1		forces can be marked as tensions and/or compressions; signs must be consistent
	$\Rightarrow T_1 = \frac{-500}{\sin 45^\circ} = -500\sqrt{2} \text{ or } -707 \text{ N}$ [magnitude = 707 N]			NB if moments are used, reaction forces at <i>C</i> , <i>D</i> must be identified for first M1
	Resolve horizontally at <i>B</i> : $T_2 + T_1 \cos 45^\circ = 0$	M1A1		
	$\Rightarrow T_2 = -T_1 \cos 45^\circ = 500 \mathrm{N}$	A1√		\checkmark their T_1
	Resolve horizontally at A^{\cdot}			
	$T_2 = T_3 \sin 30^\circ$	M1A1		
	$\Rightarrow T_3 = \frac{T_2}{\sin 30^\circ} = 1000 \mathrm{N}$	A1√	9	\checkmark their T_2
(ii)	AD and AB are in tension and could be	B1		identification of AD/AB
, í	replaced by ropes. BC is in thrust and	B1		identification of <i>BC</i> (can be implied)
	cannot be replaced by ropes.	E1	3	reference to tension/thrust
(b)	magnitude = $T_3 = 1000$ N	B1√	1	
	Total		13	

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Q	Solution	Mark	Total	Comments
4(a)	bottom right corner	M1		attempt at moments
	$W(2a) = P\cos\theta(8a)$	A1,A1		A1 each side
	$P = \frac{W}{4\cos\theta}$	A1	4	
(b)	On point of sliding			
	vertically, $N + P \sin \theta = W$	M1A1		
	horizontally, $F = P \cos \theta$	M1A1		
	friction $F = \mu N$			
	$\Rightarrow P\cos\theta = \mu (W - P\sin\theta)$	M1A1		substitute; use of $F = \mu N$
	$P\cos\theta = \mu W - \mu P\sin\theta$			
	$P(\cos\theta + \mu\sin\theta) = \mu W$			
	$P = - \mu W$	A1	7	AG
	$\cos\theta + \mu\sin\theta$,	
(c)	Slides before topples \Rightarrow			
	$\mu W < W$	M1		inequality formed
	$\cos\theta + \mu\sin\theta + 4\cos\theta$			
	$4\mu\cos\theta < \cos\theta + \mu\sin\theta$	Al		elimination of fractions / cancel W \div by $\cos \theta$ and use of $\tan \theta = 1$
	$4\mu < 1 + \mu \tan \theta$ $\tan \theta = 1 \Rightarrow 3\mu < 1$	AI M1		\Rightarrow by cost and use of tant $= 1$
	1	1011		
	$\mu < \frac{1}{3}$	A1	5	
	Total		16	
5(a)				
	$mass = m = 24a^2\rho$			
	$\therefore \rho = \frac{m}{24a^2}$	B1		use of area \times density
	Mass of strip $= 6a\delta x\rho$ MI of rectangle			
	$=\sum \frac{4}{3}(6a\delta x\rho)(3a)^2 = \sum 72a^3\rho\delta x$	M1		use of $\frac{4}{3}ml^2$
		A1		<i>m</i> , <i>l</i> correct
			1	
	$= \int_{0}^{4a} 72a^{3} \frac{m}{24a^{2}} dx$	m1		integrating - dependent on first M1

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INIU4 (cont)			40
Q	Solution	Mark	Total	Comments
5	Alternative for (a):			
	$\rho = \frac{m}{m}$	(B1)		
	$P = 24a^2$	(D1)		
	Mass of strip = $4a\delta x\rho$			
	MI of rectangle = $\sum (4a\delta x\rho)x^2$	(M1)		use of mx^2
	$= \int_0^{6a} 4a \frac{m}{24a^2} x^2 \mathrm{d}x$	(m1)		integration attempt
	$= \left[\frac{mx^3}{18a}\right]_0^{6a} = 12ma^2$	(A1, A1)	(5)	AG
(b)	$(\frac{1}{2}m) \xrightarrow{u} m$ $(\frac{3}{2}m) \xrightarrow{w} w$			
	Before After			
	angular momentum before			
	$=\frac{1}{2}mu(3a)=\frac{3mua}{2}$	M1A1		<i>ka</i> ' required for M1
	angular momentum after			
	$= lw + \frac{1}{2}m(3a)^2w$	M1		either term correct
	-1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	A1		both correct
	$=12ma^2w + \frac{9ma^2}{2}w$	B1		use of $I = 12ma^2$ anywhere
	$=\frac{33ma^2w}{m}$			
	2 use C of momentum to set			
	$3mug = 33mg^2 w$			
	$\frac{3mu}{2} = \frac{3mu}{2}$	M1		equation $-C$ of m ('their' expression)
	$\Rightarrow w = \frac{u}{11a}$	A1	7	
	Total		12	

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4 (cont	;)			300
Q	Solution	Mark	Total	Comments
6(a)	$ \begin{array}{c} \theta \\ \hline \\ T \\ \\ T \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$			
(i)	KE = $\frac{1}{2}(4m)(a\dot{\theta})^2 + \frac{1}{2}(2m)(a\dot{\theta})^2 + \frac{1}{2}(10ma^2)\dot{\theta}^2$	B1 B1		$a\dot{ heta}$ used disc KE
	$= 2ma^2\dot{\theta}^2 + ma^2\dot{\theta}^2 + 5ma^2\dot{\theta}^2$ $= 8ma^2\dot{\theta}^2$	M1 A1	4	particles KE AG
(ii)	PE lost = $4mga\theta - 2mga\theta$ = $2mga\theta$	B1		PE seen - any term
	$C \text{ of } E \Longrightarrow 8ma^2 \dot{\theta}^2 = 2mga\theta$	M1		C of E
	$a\dot{\theta}^2 = \frac{g\theta}{4}$	Al	3	AG
(b)	differentiating $2a\dot{\theta}\ddot{\theta} = \frac{g\dot{\theta}}{4}$	M1		
	$\Rightarrow a\ddot{\theta} = \frac{g}{8}$ For <i>P</i>	A1		
	$T - 2mg = 2ma\ddot{\theta} \Rightarrow T = 2mg + \frac{mg}{4} = \frac{9mg}{4}$	M1		equation for P
		A1		for $\frac{9mg}{4}$
	For <i>Q</i> ,			
	$4mg - S = 4ma\ddot{\theta} \Longrightarrow S = 4mg - \frac{mg}{2} = \frac{7mg}{2}$	M1A1		equation for Q
		A1	7	for $\frac{7mg}{2}$
	Alternative for (b): Use $C = I\ddot{H}$ for disc			
	$Sa - Ta = 10ma^2\ddot{\theta}$	(M1)		M1 for LHS attempt
	$\Rightarrow S - T = 10ma\ddot{\theta}$	(A1)		RHS correct
	For <i>P</i> , $T - 2mg = 2ma\ddot{\theta}$	(M1)		
	For Q , $4mg - S = 4ma\ddot{\theta}$	(M1)		
	Solving	(M1)		
	For S	(A1) (A1)	(7)	
	Total		14	
	TOTAL		75	